

Mathematical Lies and the Lying Liars who Teach Them

— or —

The Peano Postulates
have been Drinking,
Not Me

We Lie to Students



Precalculus: A Good Time to Stop Lying



Key Ideas



- Closure
- Identity elements
- Inverse elements

Back to the Beginning: Counting



Peano Postulates

1. $0 \in \mathbb{N}$

2. $n \in \mathbb{N} \Rightarrow n + 1 \in \mathbb{N}$



Peano Postulates

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2. $n \in \mathbb{N} \Rightarrow n + 1 \in \mathbb{N}$

3. $n + 1 = 0 \Rightarrow n \notin \mathbb{N}$

4. $n + 1 = m + 1 \Rightarrow n = m$

Peano Postulates

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2. $n \in \mathbb{N} \Rightarrow n + 1 \in \mathbb{N}$

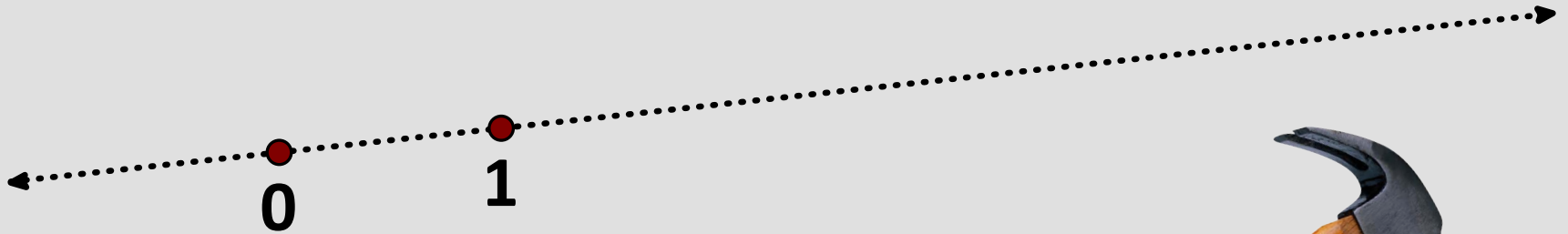
3. $n + 1 = 0 \Rightarrow n \notin \mathbb{N}$

4. $n + 1 = m + 1 \Rightarrow n = m$

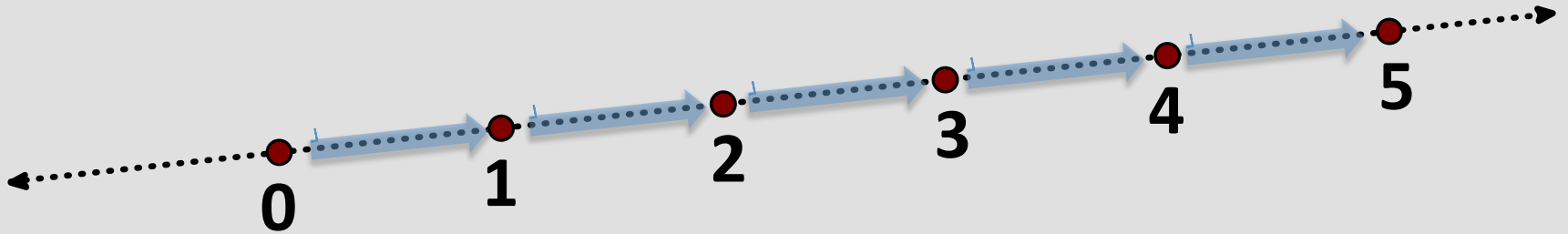
5. $0 \in S$ and $\forall n \in S, n + 1 \in S$
 $\Rightarrow S = \mathbb{N}$



Geometric Construction



Geometric Construction

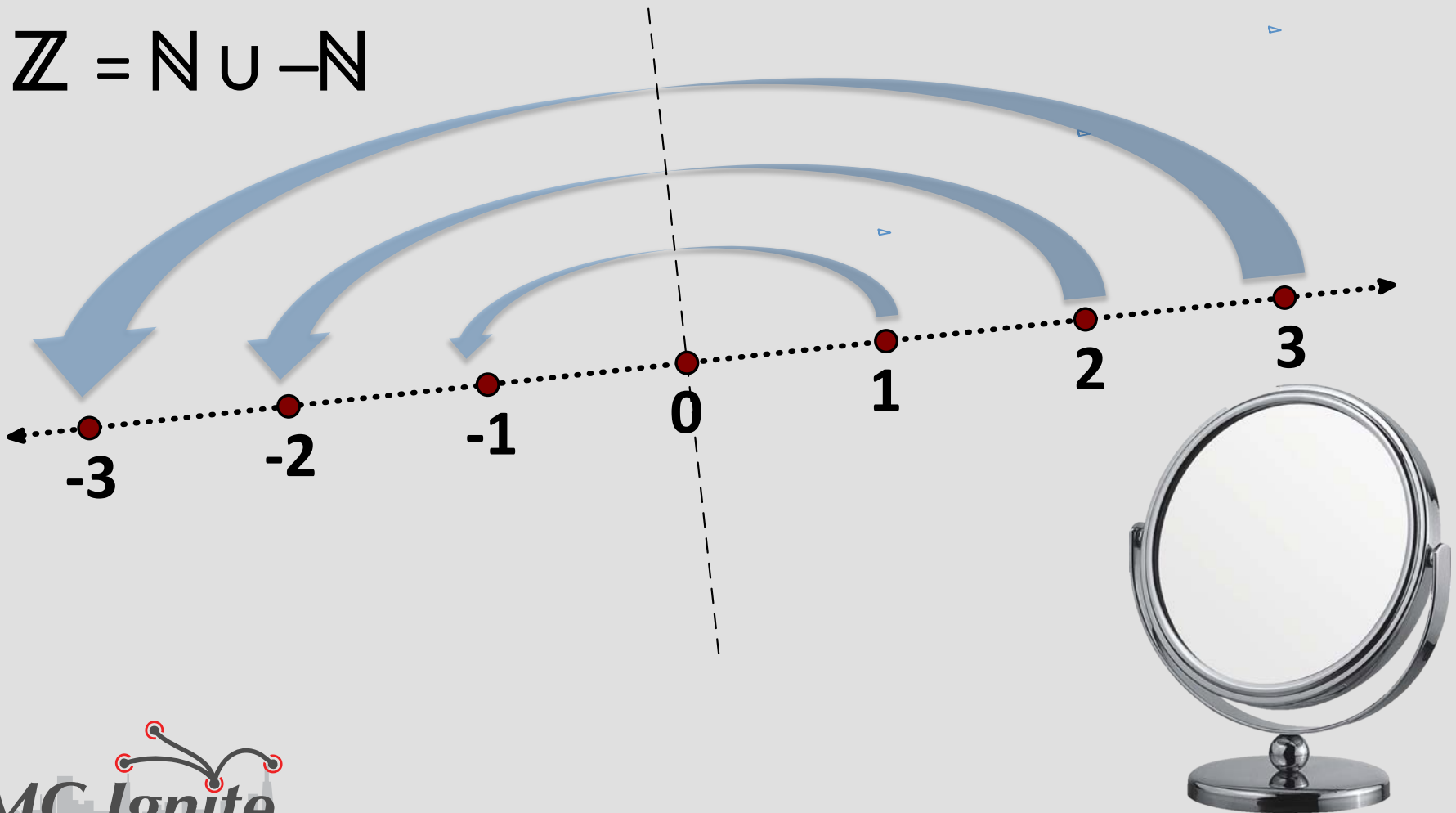


The Natural Numbers $\mathbb{N}$

N

Natural Numbers and their Opposites

$$\mathbb{Z} = \mathbb{N} \cup -\mathbb{N}$$

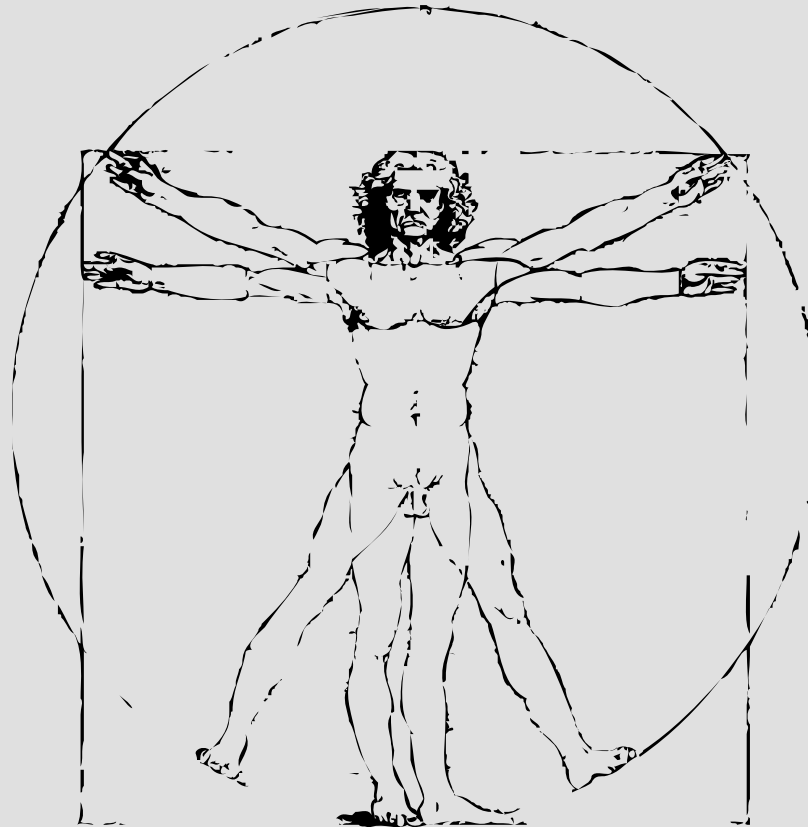


The Integers $\mathbb{Z}$



Ratios of Integers

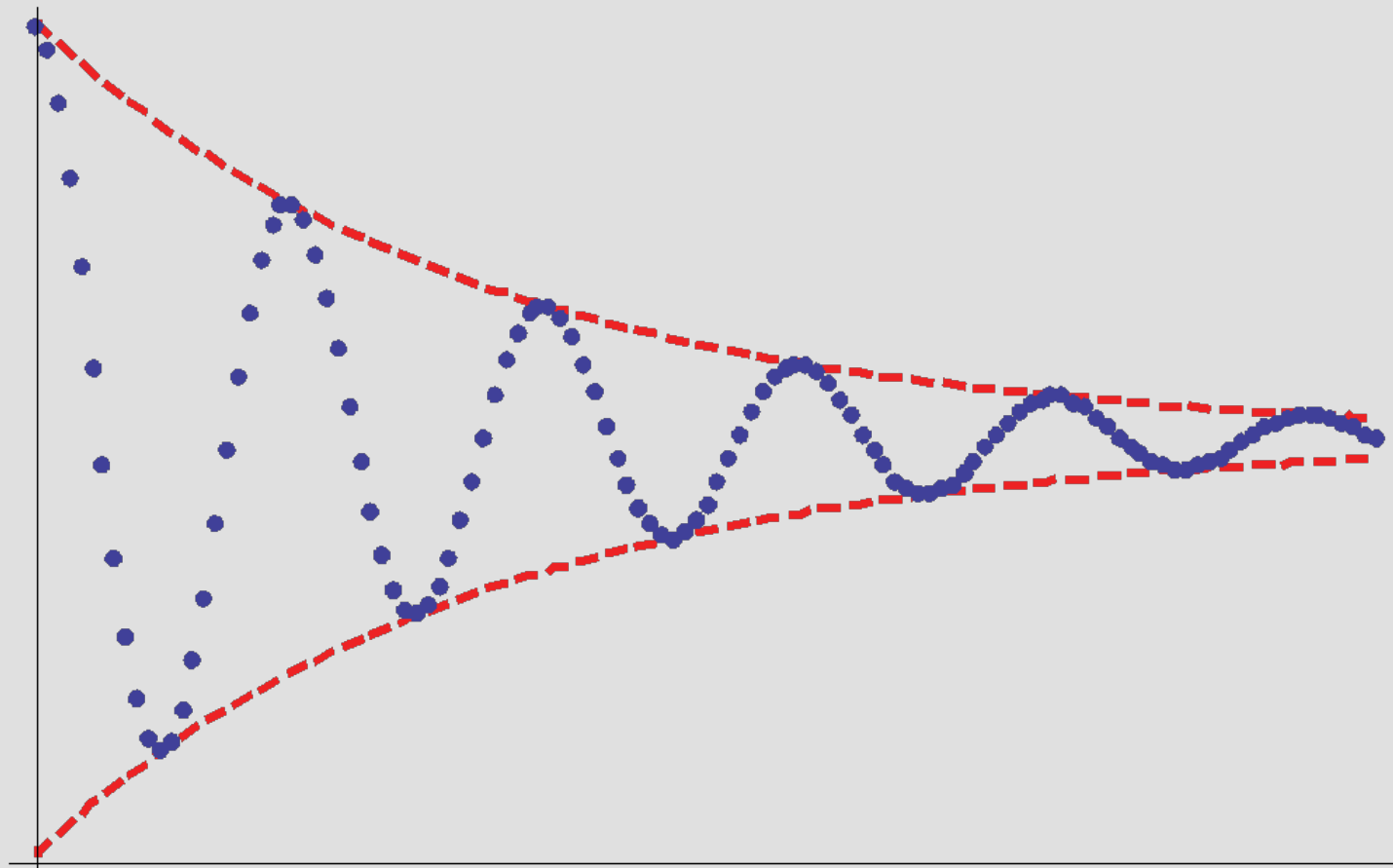
$$\mathbb{Q} = \{a/b \text{ with } a, b \in \mathbb{Z} \text{ and } b \neq 0\}$$



The Rational Numbers



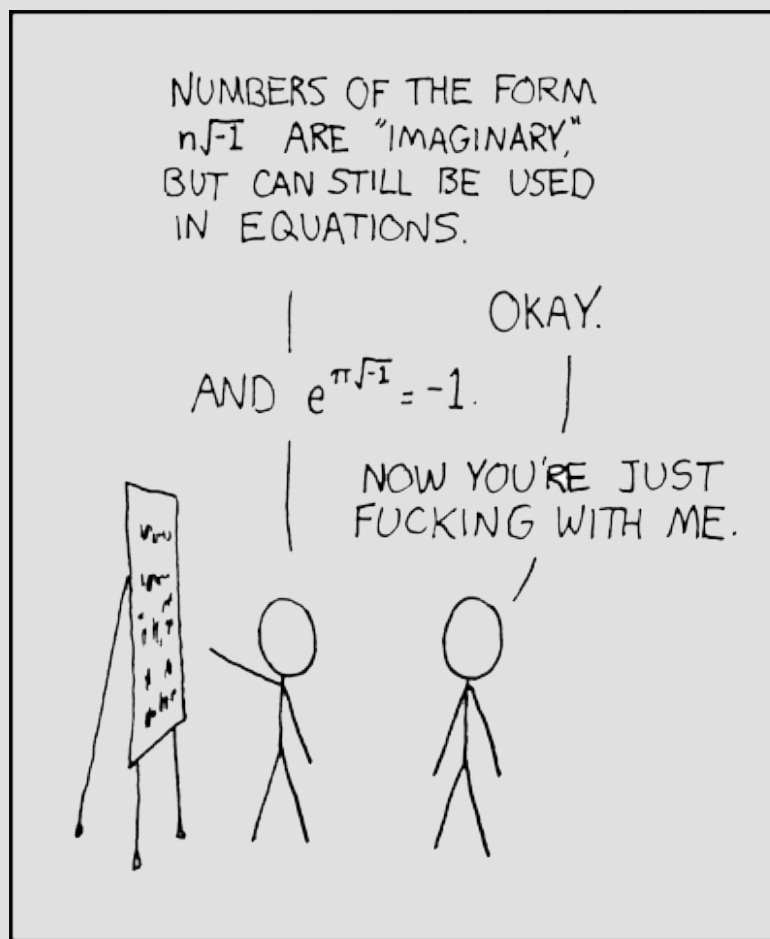
Sequences of Rational Numbers



The Real Numbers

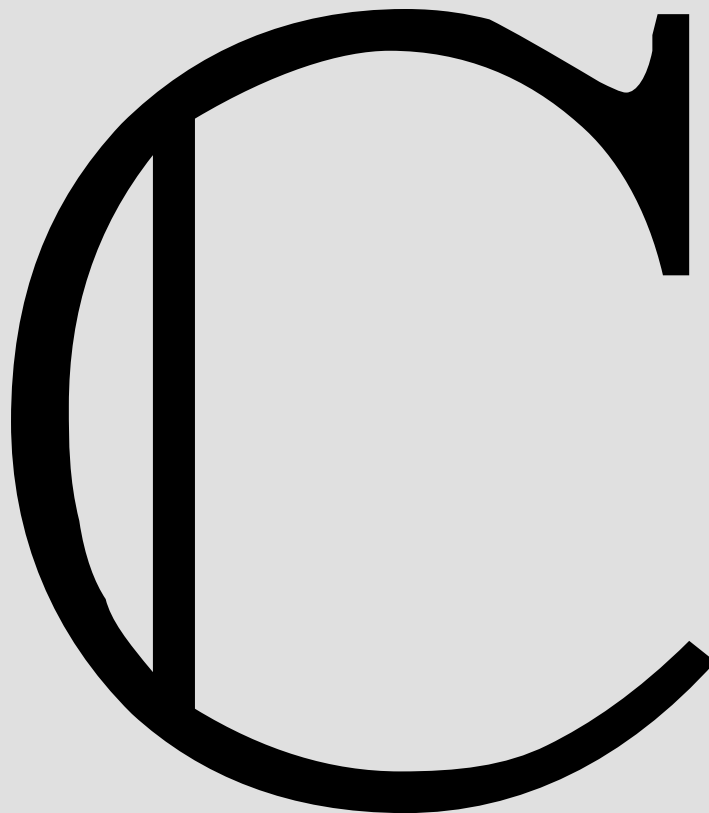
$\mathbb{R}$

Square Roots of Negative Numbers



Comic by Xkcd, <http://xkcd.com/179/>

The Complex Numbers



We're Still Lying



Time's Up!

- Apologies to Al Franken and Tom Waits for the titles.
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